

7. We choose a coordinate system as shown in the diagram. In both parts, the spider is motionless and $\vec{a} = 0$, therefore $\Sigma \vec{F} = 0$.

(a) $\Sigma \vec{F} = T\hat{j} - F_g\hat{j} = 0$, which gives

$$T = F_g = \boxed{3 \times 10^{-4} \text{ N}}$$

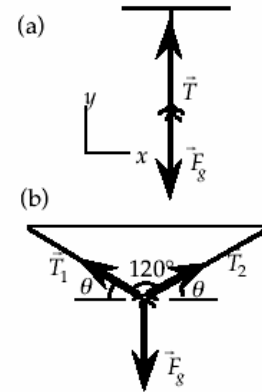
(b) $\Sigma \vec{F} = -T_1 \cos \theta \hat{i} + T_1 \sin \theta \hat{j} + T_2 \cos \theta \hat{i} + T_2 \sin \theta \hat{j} - F_g \hat{j} = 0$.

Using the two component equations, we get

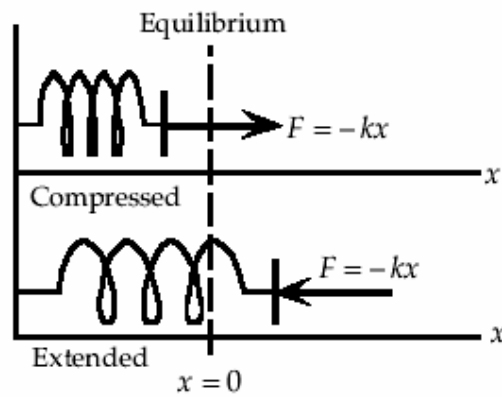
$$T_1 \cos \theta = T_2 \cos \theta, \text{ or } T_1 = T_2; \text{ and}$$

$$T_1 \sin \theta + T_2 \sin \theta = 2T_1 \sin \theta = F_g.$$

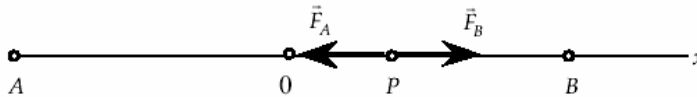
$$\text{Thus } T_1 = (3 \times 10^{-4} \text{ N}) / (2 \sin 30^\circ) = \boxed{3 \times 10^{-4} \text{ N}}$$



14.



16.



Set up a coordinate system with the origin at the midpoint of the line connecting points A and B. Consider the object (at point P), whose coordinate is x. It is a distance $L + x$ from point A and $L - x$ from point B. The forces exerted on it are $F_A = -c(L + x)$ and $F_B = c(L - x)$; so the net force is

$$F = F_A + F_B = -c(L + x) + c(L - x) = \boxed{-2cx}$$

When $x > 0$, $F < 0$ (to the right); and when $x < 0$, $F > 0$ (to the left). So F tends to pull the object back to the origin (the midpoint between A and B) where $F = 0$.

21. We need to look at horizontal forces only.

The tension in the pulled rope must be equal to the force the father exerts: $\boxed{T = F}$

If we take both sleds as the object, we get the force diagram

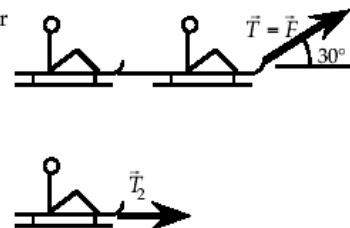
shown. Then for horizontal motion, we have

$$\Sigma F = T \cos 30^\circ = (m + m)a = 2ma, \text{ so}$$

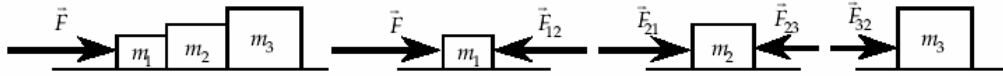
$$a = T(\cos 30^\circ) / 2m = 0.433T / m.$$

If we take the second sled as the object we get the force diagram shown. Then

$$\Sigma F = T_2 = ma, \text{ so } T_2 = m(0.433T / m) = \boxed{0.433F}$$



28. In the diagrams for the set and each of the blocks below, only the horizontal forces are shown (as vertical normal forces balance the gravity forces).



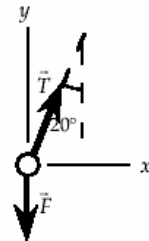
- (a) For the set we have $\Sigma F_x = ma_x$: $8.0 \text{ N} = (2.0 \text{ kg} + 3.0 \text{ kg} + 4.0 \text{ kg}) a$, which gives $a = 0.89 \text{ m/s}^2$.
- (b) For block 1 we have $\Sigma F_x = ma_x$: $F - F_{21} = m_1 a$;
 $8.0 \text{ N} - F_{12} = (2.0 \text{ kg})(0.89 \text{ m/s}^2)$, which gives $F_{12} = 6.2 \text{ N}$ to the left.
 The forces are $F = 8.0 \text{ N}$ to the right, $F_{12} = 6.2 \text{ N}$ to the left, and $F_{\text{net}1} = 1.8 \text{ N}$ to the right.
- (c) For block 2 we have $\Sigma F_x = ma_x$: $F_{21} - F_{23} = m_2 a$ and $F_{21} = F_{12}$ (Newton's third law):
 $6.2 \text{ N} - F_{23} = (3.0 \text{ kg})(0.89 \text{ m/s}^2)$, which gives $F_{23} = 3.5 \text{ N}$ to the left.
 The forces are $F_{21} = 6.2 \text{ N}$ to the right, $F_{23} = 3.5 \text{ N}$ to the left, and $F_{\text{net}2} = 2.7 \text{ N}$ to the right.
- (d) For block 3 we have $\Sigma F_x = ma_x$: $F_{32} = m_3 a$;
 $F_{32} = (4.0 \text{ kg})(0.89 \text{ m/s}^2)$, which gives $F_{32} = 3.6 \text{ N}$ to the right ($= F_{23}$, Newton's third law).
 The forces are $F_{32} = 3.6 \text{ N}$ to the right, and $F_{\text{net}3} = 3.6 \text{ N}$ to the right.

30. (a) The force acting on the table is the combined weight of the three identical blocks, so the weight of each block must be $\frac{1}{3}(3 \text{ N}) = 1 \text{ N}$. The forces exerted on block 3 are: 3 N of supporting force from the table, up; 1 N of its own weight, down; and 2 N of normal force from the other two blocks, down. The net force on block 3 is zero.
- (b) The forces exerted on block 2 are: 2 N of supporting force from block 3, up; 1 N of its own weight, down; and 1 N of normal force from the block 1, down. The net force on block 2 is zero.
- (c) The forces exerted on block 1 are: 1 N of supporting force from block 2, up; 1 N of its own weight, down. The net force on block 1 is zero.

38. From the inertial frame of Earth, for the mass we can write
 $\Sigma F_y = ma_y$: $T \cos 20^\circ - F = 0$; $T \cos 20^\circ = 6.0 \text{ N}$, which gives
 $T = 6.4 \text{ N}$; and
 $\Sigma F_x = ma_x$: $T \sin 20^\circ = ma$; $(6.4 \text{ N}) \sin 20^\circ = (2 \text{ kg})a$, which gives
 $a = 1.1 \text{ m/s}^2$.

The observer in the noninertial frame of the truck will say that there are three forces:

- $F = 6.0 \text{ N}$ in $-y$ -direction,
 T in the string $= 6.4 \text{ N}$ at 20° from $+y$, and
 a fictitious force of $(2 \text{ kg})(1.1 \text{ m/s}^2) = 2.2 \text{ N}$ toward the back of the truck.

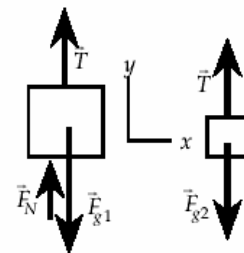


42. The coordinate system and the forces on each mass are shown. Since the system is at rest, $a = 0$ and we can write:

$$\Sigma F_y = ma_y;$$

$$T + F_N - F_{g1} = 0 \text{ for block } M \text{ and}$$

$$T - F_{g2} = 0 \text{ for block } m.$$



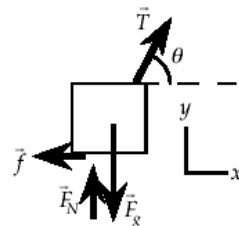
48. The coordinate system and the forces on the block are shown. Since the system is at rest, $a = 0$ and we can write:

$$\Sigma F_x = ma_x$$

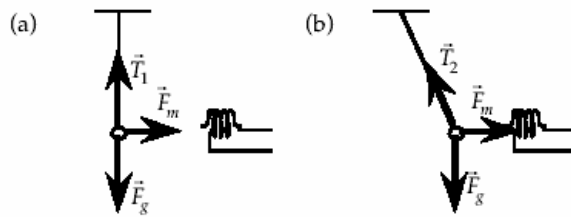
$$T \cos \theta - f = 0, \text{ which gives } f = T \cos \theta.$$

$$\Sigma F_y = ma_y$$

$$T \sin \theta + F_N - Mg = 0, \text{ which gives } F_N = Mg - T \sin \theta.$$



54.



58. We are given $\vec{F}_1 = (1.715, 0, 0)$ N, $\vec{F}_2 = (0, 1.128, 0)$ N, and $\vec{F}_3 = (F_{3x}, F_{3y}, 0)$.

(a) If the body does not accelerate, we can write $\sum \vec{F} = m\vec{a} = 0$:

For the components we get

$$x: 1.715 \text{ N} + F_{3x} = 0, \text{ which gives } F_{3x} = \boxed{-1.715 \text{ N}}$$

$$y: 1.128 \text{ N} + F_{3y} = 0, \text{ which gives } F_{3y} = \boxed{-1.128 \text{ N}}$$

$$z: 0 = 0.$$

(b) Because the forces are constant, the acceleration will be constant and we can write

$$\vec{r} = \vec{r}_0 + \vec{v}_0 t + \frac{1}{2} \vec{a} t^2, \text{ or}$$

$$(1.000, 1.000, 0) \text{ m} = (0, 0, 0) + (0, 0, 0) + \frac{1}{2} \vec{a} (5.000 \text{ s})^2, \text{ which gives } \vec{a} = (0.08000, 0.08000, 0) \text{ m/s}^2.$$

For $\sum F_x = ma_x$, we can write

$$F_1 + F_{3x} = ma_x, \text{ which gives } F_{3x} = (25.43 \text{ kg})(0.08000 \text{ m/s}^2) - 1.715 \text{ N} = \boxed{0.3194 \text{ N}}$$

For $\sum F_y = ma_y$, we can write

$$F_2 + F_{3y} = ma_y, \text{ which gives } F_{3y} = (25.43 \text{ kg})(0.08000 \text{ m/s}^2) - 1.128 \text{ N} = \boxed{0.9064 \text{ N}}$$

64. From the force diagram for the pulley and object we can write

$$\sum F_x = T_2 \cos 35^\circ - T_1 \cos 35^\circ = 0, \text{ which gives } T_1 = T_2.$$

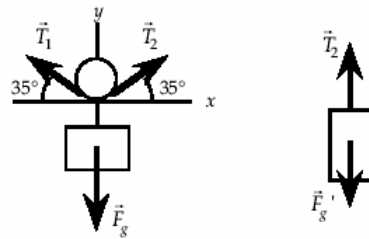
$$\sum F_y = T_1 \sin 35^\circ + T_2 \sin 35^\circ - F_g = 2T_2 \sin 35^\circ - (20 \text{ N}), \text{ which gives}$$

$$T_2 = 17.4 \text{ N}.$$

From the force diagram for the other object we can write

$$\sum F_y = T_2 - F_g' = 0, \text{ which gives}$$

$$F_g' = T_2 = \boxed{17.4 \text{ N}}$$



66. During the drop, the only force is F_g (down); during the bounce, the forces are F_g (down) and F_N (up) from the slab; during the rise, the only force is F_g (down).

If we assume a mass of 20 g,

$$F_g = (0.020 \text{ kg})(10 \text{ m/s}^2) = \boxed{0.20 \text{ N down}}$$

If the ball falls $h = 1.0$ m, the speed just before it hits is

$$v_1 = (2gh)^{1/2} = [2(10 \text{ m/s}^2)(1.0 \text{ m})]^{1/2} = 4.5 \text{ m/s}.$$

The speed just after it hits is

$$v_2 = [2g(0.80)h]^{1/2} = (0.80)^{1/2} v_1 = 4.0 \text{ m/s}.$$

If we assume the bounce occurs in 0.10 s, we can write

$$F_N - F_g = m \Delta v / \Delta t, \text{ which gives}$$

$$F_N = (0.020 \text{ kg})[4.0 \text{ m/s} - (-4.5 \text{ m/s})] / (0.10 \text{ s}) + 0.20 \text{ N} = \boxed{1.9 \text{ N up}}$$

71. We take up as positive, so $\vec{F}_g = -mg\hat{j}$, $\vec{F}_d = Av^2\hat{j}$, and $\vec{v} = -v\hat{j}$.

(a) We do a dimensional analysis of $F_d = Av^2$:

$$[F_d] = [A][v^2], [MLT^{-2}] = [A][LT^{-1}]^2, \text{ which gives } [A] = \boxed{[ML^{-1}] \text{ with units of kg/m}}$$

(b) $dv/dt = \sum F/m = (Av^2 - mg)/m = \boxed{Av^2/m - g}$.

(c) At constant velocity: $dv/dt = 0$; $(A/m)v_t^2 - g = 0$, which gives $v_t = \boxed{\sqrt{mg/A}}$.

74. Since the initial speed is $2 \times 10^6 \text{ m/s}$, the time the electron spends between the plates will be short and we will neglect the vertical acceleration $-g$ and assume that the vertical motion has constant velocity.

From $\sum \vec{F} = m\vec{a}$, we get

$$\sum F_y = ma_y; \sum F_x = ma_x: \quad 0 = a_y; \quad F = ma_x.$$

- (a) For the vertical motion: $y = v_y t$; $1 \times 10^{-2} \text{ m} = (2.0 \times 10^6 \text{ m/s})t$, which gives

$$t = \boxed{5 \times 10^{-9} \text{ s}}$$

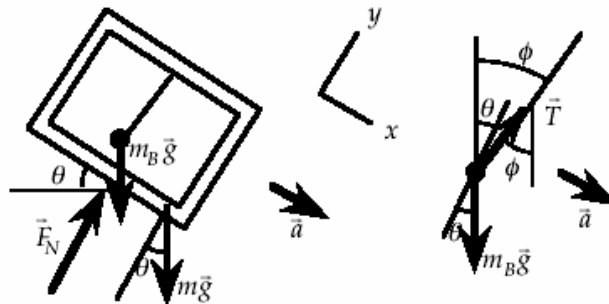
- (b) We can find the horizontal acceleration from $\sum F_x = ma_x$:

$$a_x = (3.0 \times 10^{-18} \text{ N}) / (9.0 \times 10^{-31} \text{ kg}) = 3.3 \times 10^{12} \text{ m/s}^2.$$

Since the acceleration is constant, the velocity is found from

$$v_x = v_{0x} + a_x t = 0 + (3.3 \times 10^{12} \text{ m/s}^2)(5.0 \times 10^{-9} \text{ s}) = \boxed{1.7 \times 10^4 \text{ m/s}}$$

77.



From the force diagram for the system of the frame and plumb bob, we can write

$$\sum F_x = ma_x:$$

$$(m_B + m)g \sin \theta = (m_B + m)a; \quad \text{and}$$

$$\sum F_y = ma_y:$$

$$F_N - (m_B + m)g \cos \theta = 0.$$

From the x -equation we find

$$a = g \sin \theta.$$

From the force diagram for the system of the plumb bob, we can write

$$\sum F_x = ma_x:$$

$$m_B g \sin \theta + T \sin (\phi - \theta) = m_B a; \quad \text{and}$$

$$\sum F_y = ma_y:$$

$$T \cos (\phi - \theta) - m_B g = 0.$$

Using $a = g \sin \theta$ in the x -equation, we find $\sin (\phi - \theta) = 0$, so $\boxed{\phi = \theta}$.