

## 2002S Homework #04

Due 05/07/2002

1. For a hydrogen atom in a uniform electric field, show that the energy of a state with  $l=n-1$ ,  $m=n-1$  does not change to the first order in the field.
2. A plane rotator with moment of inertia  $I$  (thus its unperturbed Hamiltonian  $H_0 = L_z^2/2I$ ) and electric dipole moment  $\mathbf{d}$  is placed in a uniform electric field  $\mathbf{E}$ , in the plane of rotation. Consider  $\mathbf{E}$  to be a perturbation and evaluate the first non-vanishing correction to the energy levels of the rotator.  
*Hint:* you have to calculate to the second order in perturbation.
3. The Hamiltonian for an electron in a hydrogen atom subject to a constant magnetic field  $\mathbf{B}$ , is, with the neglect of spin,  $H = \frac{\vec{p}^2}{2m} - \frac{e^2}{r} + \left(\frac{e}{2mc}\right)\vec{L}\cdot\vec{B}$ , where  $\mathbf{L}$  is the angular momentum operator. In the absence of the magnetic field, there will be a single line in the transition from an  $(n=4, l=3)$  to an  $(n=3, l=2)$  state. What will be the effect of the magnetic field on that line? Sketch the new spectrum and the possible transitions. How many lines will there be?