9. We choose the coordinate system shown, with positive torques clockwise. As the plank is moved out from the roof, the effective normal force acts at a point closer to the edge. When the normal force reaches the edge, the plank is on the verge of tipping. We write $\sum \tau = I \theta$ about the edge $A$ from the force diagram for the plank, the load and the concrete:

$$\sum \tau = M_1g(L-x) = 0,$$

which gives

$$x = M_1L/(M_1 + M_2) = (15 \text{ kg})(2.4 \text{ m})/(30 \text{ kg} + 15 \text{ kg}) = 0.8 \text{ m}$$

We choose the coordinate system shown, with positive torques counterclockwise.

(a) We write $\sum \tau = I \theta$ about the point $B$ from the force diagram for the ladder and man:

$$\sum \tau = mgL \sin \theta + M_2g \sin \theta - F_{\text{bottom}} \sin \theta = 0.$$  

We write $\sum F_y = m \dot{y}$ from the force diagram for the ladder and man:

$$F_{\text{bottom}} = m g \sin \theta = 0.$$  

We write $\sum F_x = m \dot{x}$ from the force diagram for the ladder and man:

$$F_{\text{bottom}} - (m + M_2) g = 0.$$  

As the man climbs the ladder, the friction force at the bottom increases. At the point where slipping begins,

$$F_{\text{bottom}} = F_{\text{bottom max}} = \mu (m + M_2) g.$$  

Then we have

$$F_{\text{bottom}} = \mu (m + M_2) g.$$  

Using these in the torque equation, we get

$$d = [(m + M_2)L g \sin \theta]/[(m + M_2) g \sin \theta] = 2.5 \text{ m}.$$  

(b) We write $\sum \tau = I \theta$ about the point $A$ from the force diagram for the ladder and man:

$$\sum \tau = F_{\text{bottom}} \sin \theta - M_2g \sin \theta - F_{\text{bottom}} \sin \theta = 0.$$  

We write $\sum F_y = m \dot{y}$ about the point $O$ from the force diagram for the ladder and man:

$$\sum F_x = F_{\text{bottom}} \sin \theta - M_2g \sin \theta - F_{\text{bottom}} \sin \theta = 0.$$  

We can combine these three torque equations to obtain the force equations.

If we add the equations for points $A$ and $O$, we get

$$F_{\text{bottom}} = F_{\text{bottom}},$$  

which is the $x$-equation.

If we subtract the equations for points $B$ and $O$, we get

$$F_{\text{bottom}} = \mu (m + M_2) g,$$  

which is the $y$-equation.

27. The force $F$ supplies a counterclockwise torque about the axis of the pulleys, $\tau_1 = FR_1$, where $R_1 = 20 \text{ cm}$ while the weight of the engine (of mass $m$) exerts a clockwise torque about the axis, $\tau_2 = -mgR_2$, where $R_2 = 8.0 \text{ cm}$. To balance the torques, set

$$\sum \tau = FR_1 - mgR_2 = 0,$$  

which gives

$$F = mgR_2 / R_1 = \frac{(300 \text{ kg})(9.8 \text{ m/s})^2(8.0 \text{ cm})}{20 \text{ cm}} = 1.2 \text{ kN}.$$  

38. See the diagram below. The block must be brought to such a position that its center of mass (point $O$) is directly above the axis of rotation (through point $A$). The critical angle in question is

$$\theta = \frac{cm^2}{(cm/h)}.$$  

The work $W$ done must be at least equal to the increase in gravitational potential energy of the block (assuming that the block virtually stops at the critical position). Since the center of mass rises by $\Delta h = \frac{h}{2}$, the work is

$$W_{\text{min}} = mg \Delta h = mg \left[ \left( \frac{h}{2} \right)^2 + \left( \frac{cm}{cm} \right)^2 \right] - \frac{h}{2}.$$
42. We choose the coordinate system shown, with positive torques clockwise.
(a) We write \( \sum \tau = \tau A \) about the point A from the force diagram for the rock:
\[
\sum \tau = F_{A}R \sin \theta - f_{s}(R + R \cos \theta) = 0,
\]
which gives
\[
f_{s} = \sin \theta / (1 + \cos \theta)F_{N} = \tan(\theta)F_{N}.
\]
The larger the angle becomes the greater the friction force required. The maximum friction force is \( f_{s,\text{max}} = \mu_{s}F_{N} \), so we find the maximum angle from
\[
\tan(\theta_{\text{max}}) = f_{s,\text{max}} / F_{N} = \mu_{s} = 0.6,
\]
which gives
\[
\theta_{\text{max}} = \arctan(0.6).
\]
(b) We write \( \sum \tau = \tau A \) about the point B from the force diagram for the rock:
\[
\sum \tau = T(R + R \cos \theta) - mgR \sin \theta = 0,
\]
which gives
\[
T = \sin \theta \theta_{\text{max}} / (1 + \cos \theta_{\text{max}})mg
\]
\[
= \tan(\theta_{\text{max}})mg = \mu_{s}mg
\]
\[
= (0.6)(1088 \text{ kg})(9.8 \text{ m/s}^2) = 6x10^3 \text{ N}
\]
(c) When the angle is less than the maximum angle, from part (b) we get
\[
T = \mu_{s}mg \tan(\theta).
\]

59. We call the length of the beam \( L_{\text{beam}} \). The initial length of the cable is
\( L_{0} = L_{\text{beam}} / \cos 30^\circ = 2L_{\text{beam}} / \sqrt{3} \) and the distance along the wall from the beam to the cable is \( D = L_{\text{beam}} \tan 30^\circ = L_{\text{beam}} / \sqrt{3} \). When the load is hung at the end of the beam, there must be an additional tension in the cable to maintain equilibrium:
\[
\sum \tau_{\text{beam}} = (\Delta \tau) \sin 30^\circ = -M_{G}L_{\text{beam}},
\]
which is an additional stress:
\[
\Delta \tau / \sqrt{3} = 588 \text{ N}/[\sqrt{10^4 \text{ m}^2/\text{s}^2}] = 1.87 \times 10^3 \text{ N/m}^2.
\]
(Note that even when the additional tension is added, this is less than the tensile strength, so the cable does not break.)

The additional stress produces an elongation of the cable:
\[
\Delta L / L_{0} = \Delta \tau / \gamma Y.
\]
This elongation causes the beam to drop below the horizontal (exaggerated in the diagram). We find the angle \( \theta \) from a geometrical formula for a triangle:
\[
\Delta \theta / \Delta L_{\text{beam}} = 2 \theta_{\text{beam}} \cos \theta = (L_{0} + \Delta L)^2 = L_{0}^2(1 + 2 \Delta L / L_{0}),
\]
where we have used the fact that \( \Delta L << L_{0} \). Because \( \Delta L^2 = L_{0}^2 \), this becomes
\[
-2L_{\text{beam}} / \sqrt{3} \theta_{\text{beam}} \cos \theta = 2(\Delta L) / L_{0} = 2 \Delta L / L_{0},
\]
which reduces to
\[
\cos \theta = (4 \gamma Y)/(3(588)) = 0.00206 \text{, which gives } \theta = 90.12^\circ.
\]
Thus the beam is 912° below the horizontal.
We choose the coordinate system shown, with positive torques counterclockwise.

(a) We write $\sum T = I\alpha$ about the point $A$ from the force diagram for the beam:
$$\sum T_A = Mg(\frac{1}{4}L \cos \theta_A - TL \sin \theta_A) = 0,$$
which gives $T = \frac{Mg \cot \theta_A}{4}.$

(b) When the cable snaps, the tension is zero, so we have
$$\sum T_A = I\alpha,$$
$$Mg(\frac{1}{4}L \cos \theta_A) = \frac{1}{4}ML^2 \alpha,$$ which gives $\alpha = \frac{3g \cos \theta_A}{2L}.$

(c) The angular acceleration is not constant. Rather than integrate, we use the work-energy theorem, with the reference level for potential energy at the horizontal position. No work is done by the force at the pivot, so we have
$$W = \Delta K + \Delta U,$$
$$0 = (\frac{1}{2}I_A \omega^2 - 0) + Mg(0 - \frac{1}{4}L \sin \theta_A).$$
When we use $I_A = \frac{1}{2}ML^2,$ we get $\omega = \sqrt{3g \sin \theta_A}/L.$

75. We choose the coordinate system shown, with positive torques clockwise. We write $\sum T = I\alpha$ about the point $A$ from the force diagram for the cylinder:
$$\sum T_A = F_N \sin \theta - f_s (R + R \cos \theta) = 0,$$ which gives
$$f_s = [\sin \theta / (1 + \cos \theta)] F_N \tan (\frac{1}{4} \theta) = F_N.$$
Because $f_s = \mu_s F_N,$ the minimum value of $\mu_s$ is when $f_s = \mu_s F_N.$ So
$$\mu_{min} = \frac{\tan (\frac{1}{4} \theta)}{F_N},$$
which gives
$$\mu_{min} = \tan (\frac{1}{4} \theta).$$

77. The net force exerted on the ball is zero, so
$$F_{N_A} - T \sin \theta = 0 \quad \text{in the horizontal direction and}$$
$$f + T \cos \theta = mg = 0 \quad \text{in the vertical direction.}$$
Also, the net torque about point $A$ must vanish. The lever arm of $T$ about point $A$ is $AD = CA \sin \theta = CB \sin \theta,$ and that of the weight of the ball is $R,$ its radius. Here $\theta = \sin^{-1}(11 \text{ cm} / 90 \text{ cm}) = 7.02^\circ.$ Thus
$$\sum T_A = T (CB \sin \theta) = mgR = 0.$$
And when $\mu$ is at its smallest possible value
$$f = f_{min} = \mu F_{N_A}.$$ Combine these equation to obtain
$$\mu = \cot \theta = 90 \text{ cm} / 60 \text{ cm} - \cot 7.02^\circ = 0.88.$$